

Inference Rules as Strategies

This is an articulation of the eight inference rules as strategies in the reverse method. The reverse method instills a habit of approaching problems with *goal-oriented* strategies.

The most important feature of this method is its basis in wants and needs. Strategies are driven by what is desired, that is, by what you *want*. Knowledge of what you *need* comes out of your understanding of what you want.

NOTE: “Introduction” means it builds a statement
 “Elimination” means it breaks apart a statement

And Introduction: *Conjunction* (Conj)

If you want a conjunction on a line ($\square \bullet \triangle$), then introduce it.
You’ll need \square on one line, and \triangle on a separate line.

Want $\square \bullet \triangle$, then need \square as well as \triangle .

And Elimination: *Simplification* (Simp)

If you want part of a conjunction on a line (i.e. one of the conjuncts \square , \triangle), then you can *simply* take it.

Want \square or \triangle , have $\square \bullet \triangle$, take it!

Or Introduction: *Addition* (Add)

If you want a disjunction on a line ($\square \vee \triangle$), then introduce it.
You’ll need \square on a line, or \triangle on a line.

Want $\square \vee \triangle$, then need \square or \triangle .

Or Elimination: *Disjunctive Syllogism* (DS)

If you want part of a disjunction on a line (i.e. one of the disjuncts \square, \triangle), then eliminate the disjunction and take the part you want. You’ll need the negation of one of its disjuncts $\sim \square$ or $\sim \triangle$ on a line.

Want \square or \triangle , have $\square \vee \triangle$, then need $\sim \square$ (for \triangle) or $\sim \triangle$ (for \square)

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Or Introduction: *Constructive Dilemma* (CD)

If you want a disjunction on a line ($\bigcirc \vee \star$), then introduce it the hard way. You'll need two conditionals whose antecedents (their \square s) are the disjuncts of the disjunction ($\square \vee \triangle$), and whose consequents (their Δ s) are the disjuncts of the disjunction desired ($\bigcirc \vee \star$), all on separate lines.

Want $\bigcirc \vee \star$, then need $\square \rightarrow \bigcirc$, as well as $\triangle \rightarrow \star$, and $\square \vee \triangle$

Conditional Elimination: *Modus Ponens* (MP)

If you want the consequent (the Δ) of a conditional ($\square \rightarrow \Delta$) on a line, then eliminate the conditional and cleanly get the consequent. You'll need the antecedent (the \square) on a separate line to take the consequent.

Want Δ , have $\square \rightarrow \Delta$, then need \square .

Conditional Elimination "Backwards": *Modus Tollens* (MT)

If you want the antecedent (the \square) of a conditional ($\square \rightarrow \Delta$) on a line, then that's just too bad, you'll never get it! If, however, you want the *negation* of the antecedent ($\sim \square$) on a line, then eliminate the conditional and get it. You'll need the negation of the consequent ($\sim \Delta$) on a separate line to take the negation of the antecedent.

Want $\sim \square$, have $\square \rightarrow \Delta$, then need $\sim \Delta$.

Conditional Introduction: *Hypothetical Syllogism* (HS)

If you want the conditional ($\square \rightarrow \bigcirc$) on a line, then introduce it by building it from two other conditionals. You'll need one conditional on a line that "starts" with the antecedent you're trying to build (i.e. \square), and you need another conditional on a separate line that "ends" with the consequent of the conditional you're trying to build (i.e. \bigcirc). Also, *both* conditionals must "share" a common element Δ , as the consequent of first and as the antecedent of the second.

Want $\square \rightarrow \bigcirc$, then need $\square \rightarrow \Delta$ as well as $\Delta \rightarrow \bigcirc$.